

SURVEY OF INDETERMINACIES OF FITTING PARAMETERS IN MOLECULAR SPECTROSCOPY. I. THEORY AND SIMPLE EXAMPLES.

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Effective Hamiltonians $H(\mathbf{q}, \mathbf{p}, \mathbf{s}, \mathbf{i}; \mathbf{c})$ of molecules depend on the dynamical variables $\mathbf{q}, \mathbf{p}, \mathbf{s}, \mathbf{i}$, and on a set of parameters (or 'constants') \mathbf{c} . The latter can be given a theoretical significance by perturbation theory, but they are usually treated as adjustable parameters to be fitted to an observed spectrum, or in effect fitted to the eigenvalues of H . Such fits are used as tests of spectroscopic assignments. If H has the property that a transformation UHU^{-1} by a unitary operator U produces a Hamiltonian $H(\mathbf{q}, \mathbf{p}, \mathbf{s}, \mathbf{i}; \tilde{\mathbf{c}})$ which is identical in form to the original Hamiltonian with a different set of parameters $\tilde{\mathbf{c}}$, then \mathbf{c} is indeterminate because both \mathbf{c} and $\tilde{\mathbf{c}}$ correspond to the same set of eigenvalues. In such cases the Hamiltonian has a generalized type of symmetry, because it commutes with operators that act on both the variables and the parameters. Typically U is taken in the form e^{iS} , where S is Hermitian and of odd degree in the momenta and angular momenta. Examples of such indeterminacies of \mathbf{c} are given for the vibration-rotation spectra of diatomic molecules.