Microwave spectra have been recorded for the \( C_{3v} \) symmetric complexes \( \text{Kr-SO}_3 \) and \( \text{Kr-SO}_3\text{-CO} \). The Kr-S distances are 3.438(3) Å in \( \text{Kr-SO}_3 \) and 3.488(6) Å in \( \text{Kr-SO}_3\text{-CO} \). Thus, the addition of CO to \( \text{Kr-SO}_3 \) increases the Kr-S distance by 0.050(9) Å. In contrast, the C-S distance in the trimer, 2.871(9) Å, is the same as that previously determined for \( \text{SO}_3\text{-CO} \) to within the estimated uncertainties. Observed values of the \(^{83}\text{Kr}\) nuclear quadrupole coupling constants provide direct probes of the electric field gradient at the Kr nucleus. We find that, although the Kr and CO in the trimer are on opposite sides of the \( \text{SO}_3 \) and are thus not in direct contact, the addition of CO to \( \text{Kr-SO}_3 \) reduces the electric field gradient at the Kr nucleus by 18%. Calculations using the Block Localized Wavefunction decomposition method are used to understand the physical origins of this change. While the magnitudes of both the electric field and the electric field gradient at the Kr nucleus decrease upon addition of the CO to \( \text{Kr-SO}_3 \), the changes arise from different and rather complex combinations of geometrical distortion, electrostatic, polarization, and electron transfer effects. For the electric field gradient, polarization and structural change in the \( \text{Kr-SO}_3 \) make the primary contributions while for the electric field itself, the change in the electrostatic contribution has the largest effect. The calculated binding energies are additive, with that of the trimer very nearly equal to the sum of the binding energies of \( \text{Kr-SO}_3 \) and \( \text{SO}_3\text{-CO} \).